

Automatic selection of the number of clusters using Bayesian clustering and sparsity-inducing priors

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Abstract

Clustering is a ubiquitous task in ecological and environmental sciences and multiple methods have been developed for this purpose. Because these clustering methods typically require users to a priori specify the number of groups, the standard approach is to run the algorithm for different numbers of groups and then choose the optimal number using a criterion (e.g., AIC or BIC). The problem with this approach is that it can be computationally expensive to run these clustering algorithms multiple times (i.e., for different numbers of groups) and some of these information criteria can lead to an overestimation of the number of groups. To address these concerns, we advocate for the use of sparsity-inducing priors within a Bayesian clustering framework. In particular, we highlight how the truncated stick-breaking (TSB) prior, a prior commonly adopted in Bayesian nonparametrics, can be used to simultaneously determine the number of groups and estimate model parameters for a wide range of Bayesian clustering models without requiring the fitting of multiple models. We illustrate the ability of this prior to successfully recover the true number of groups for three clustering models (two types of mixture models, applied to GPS movement data and species occurrence data, as well as the species archetype model) using simulated data in the context of movement ecology and community ecology. We then apply these models to armadillo movement data in Brazil, plant occurrence data from Alberta (Canada), and bird occurrence data from North America. We believe that many ecological and environmental sciences applications will benefit from Bayesian clustering methods with sparsity-inducing priors given the ubiquity of clustering and the associated challenge of determining the number of groups. Two R packages, EcoCluster and bayesmove, are provided that enable the straightforward fitting of these models with the TSB prior.

KEYWORDS

Bayesian nonparametrics, biogeographic region model, clustering, mixture model, movement ecology, species archetype model

INTRODUCTION

Clustering algorithms are commonly used across multiple disciplines to reduce data dimensionality by grouping data items with similar features, enabling the identification of the main latent structural characteristics of highly multivariate data (Berkhin, 2006; Jain et al., 1999; Legendre & Legendre, 2012). In environmental sciences and ecology, clustering approaches have been extensively used since at least the 1920s (Legendre & Legendre, 2012). Examples for biodiversity data sets include cluster analysis to define biogeographical regions (Azeria et al., 2007; Foster et al., 2017; Kreft & Jetz, 2010; Lyons et al., 2017), identify indicator species by grouping species that tend to co-occur (Azeria et al., 2009), identify microbial community patterns associated with sample origin and/or sampling time (Ramette, 2007), and cluster species that tend to have similar relationships with other species in food web studies (e.g., set of predator species that feed on the same set of prey species; Baskerville et al., 2011). Cluster analysis has also been extensively used in other environmental science applications. For example, clustering has been used to classify water catchments in data-scarce regions (Auerbach et al., 2016) and to understand the spatial variation in the detection rate of pharmaceuticals in rivers across different regions (Jameel et al., 2020).

Clustering is an important task across scientific fields and, as a result, a rich assortment of methods and algorithms have been developed through time (Jain et al., 1999). These methods can be classified based on several dichotomies, such as whether a single partition (partitional) or a nested series of partitions (hierarchical) is created, if methods output hard (each data item can only belong to a single group) or fuzzy (each data item can have varying degree of membership to each group) groups, and if these methods are algorithmic or probabilistic (Berkhin, 2006; Bouveyron & Brunet-Saumard, 2014; Jain et al., 1999; Legendre & Legendre, 2012; Saxena et al., 2017). A long-term challenge when using clustering algorithms consists of defining the appropriate number of clusters, which typically has to be a priori specified (Berkhin, 2006; Jain et al., 1999; Legendre & Legendre, 2012; Saxena et al., 2017). The standard approach for this task is to systematically vary the number of groups and run the algorithm once for each setting. Then, the optimal number of groups is determined using a performance metric (e.g., AIC, BIC, gap statistic, integrated classification likelihood, minimum message length; Berkhin, 2006; Biernacki et al., 2000; Charrad et al., 2014; Daudin et al., 2008; Depraetere & Vandebroek, 2014; Fraley & Raftery, 2007; Hui et al., 2013; Hui & Warton, 2015; Lyons et al., 2017; ter Braak et al., 2003; Tibshirani et al., 2001). This approach has been extensively used in the past but it can be computationally

expensive and time consuming for large data sets and/or complex models. Importantly, large simulation studies have shown that no single performance metric is consistently better than the others (Depraetere & Vandebroek, 2014) and that some of these commonly adopted information criteria tend to favor models with a larger number of groups than warranted (Casella et al., 2014), even if the model faithfully mirrors the data-generating mechanism (Pohle et al., 2017).

The generation of sparse solutions (i.e., where only a small fraction of the parameters are non-zero) is highly desirable for a range of modeling applications. For example, regularization (i.e., penalty terms added to the objective function) in statistical (e.g., regression) and machine learning (e.g., support vector machines) models is key to avoid overfitting, increase predictive skill, and improve interpretability of model results. Interestingly, many of the proposed regularization approaches can be interpreted as Bayesian models with very specific types of sparsity-inducing priors (Hahn & Carvalho, 2015; Hooten & Hobbs, 2015; Park & Casella, 2008; Wood, 2017). Likewise, the challenge of determining the number of clusters can also be tackled by defining Bayesian models with sparsity-inducing priors (i.e., priors that favor fewer clusters). In this paper, we describe how different types of Bayesian clustering methods applied to ecological data, when used together with sparsity inducing priors, can automatically determine the number of clusters without requiring fitting multiple models. In particular, we focus on a specific type of sparsity-inducing prior, the truncated stick-breaking (TSB) prior (i.e., an approximation of the Dirichlet Process), that has been extensively used in Bayesian nonparametrics (Sethuraman, 1994) but that has seen relatively little application in ecological and environmental sciences.

To illustrate how this approach can be used for a range of models, we rely on three Bayesian clustering methods applied to ecological data: two types of mixture models, applied to movement and species occurrence data, and the species archetype (SA) model (Dunstan et al., 2013). To our knowledge, none of the three clustering methods with the TSB prior has been used in ecological applications. We apply these three clustering methods to simulated data to showcase the ability of the sparsity-inducing priors to successfully recover the true number of groups by fitting the model just once. We then perform an exploratory data analysis with these methods to reveal the latent structure in armadillo movements in the Pantanal wetlands (Brazil), plant occurrence in Alberta (Canada), and breeding bird occurrence from United States and Canada. We also provide two R packages (EcoCluster and bayesmove) that enable straightforward fitting of these clustering models, which we expect will be of broad use for ecological and environmental science clustering tasks.

MATERIALS AND METHODS

Truncated stick-breaking prior

Clustering methods (also referred to as mixture models; McLachlan & Peel, 2000) explicitly or implicitly contain multiple latent variables z_i , $i = 1, \dots, n$. The latent variable z_i indicates the cluster membership of unit i and can take on any integer value between 1 and K , where K is the number of clusters defined a priori by the user. Depending on the specific application, this unit can consist of individual forest plots, rivers, species, pharmaceuticals, sampling points, etc. In probabilistic clustering approaches, it is typically assumed that the latent variable z_i follows a categorical distribution:

$$z_i \sim \text{Cat}(\boldsymbol{\theta})$$

where the vector $\boldsymbol{\theta}$ is of size K (i.e., the number of clusters) and contains probabilities that sum to 1, indicating the likelihood that unit i is assigned to individual clusters. This categorical distribution is used because it is assumed each unit can only belong to a single group.

Finding the optimal number of groups K by fitting the model multiple times (once for each K value) and choosing K using a model selection criterion such as AIC or BIC can be a prohibitive approach if fitting each model is computationally expensive. Furthermore, past research has suggested that some of these information criteria tend to favor models with a larger number of groups than warranted (Casella et al., 2014), even if the model faithfully mirrors the data-generating mechanism (Pohle et al., 2017). The approach proposed here avoids these problems by relying on the TSB prior, a particular type of prior for $\boldsymbol{\theta}$ that favors sparseness (i.e., a smaller number of groups). With this prior, the user is only required to specify the maximum number of groups K and the algorithm chooses the number of groups ($k \leq K$) that best clusters the sample data.

The stick-breaking prior has a long tradition in Bayesian nonparametric models. This prior arises from the Dirichlet process (DP), which is arguably the most popular Bayesian nonparametric model used for clustering applications (Ferguson, 1973). The distribution over random partitions induced by the DP is commonly known in the machine learning community as the Chinese restaurant process (CRP; Teh, 2011) and is equivalent to the Ewens sampling formula used to describe a distribution over partitions in population genetics that was introduced before the DP (Crane, 2016; Ewens, 1972). Another definition of the DP is the Pólya urn representation, which essentially describes the same distribution from

the CRP (Blackwell & MacQueen, 1973). Here, we focus on the alternative definition of the Dirichlet process known as the “stick-breaking” construction (Sethuraman, 1994). This definition of the DP model is considerably simpler and more general than the previously mentioned representations. This approach has been extremely useful for the development of novel statistical models as well as new Markov Chain Monte Carlo (MCMC) inference algorithms (Ishwaran & James, 2001). Notice that, despite similar names, this “stick-breaking” prior is not associated with the “broken stick model” for species abundance described in MacArthur (1957).

As commonly done in Bayesian nonparametrics (Ishwaran & James, 2001), we adopt a truncated version of this prior by defining a maximum number of groups (hereafter referred to as the truncated stick-breaking [TSB] prior). To define the maximum number of groups, the standard advice is to choose a truncation point such that the results would be indistinguishable from what would have been obtained with a larger number of groups (Ishwaran & James, 2001). More practically, as long as most of the posterior mass is concentrated on the initial components, then the actual value for the maximum number of groups should have no effect on model results (Manrique-Vallier, 2016). On the other hand, if the maximum number of clusters is reached, then the standard advice is to increase the maximum number of possible groups to avoid an incorrect approximation. Notice that, because the TSB prior is typically viewed as an approximation to the DP, some researchers actually prefer to work directly with the DP to avoid any potential approximation errors (MacEachern & Muller, 1998; Papaspiliopoulos & Roberts, 2008).

Instead of viewing the TSB prior solely as an approximation to the DP, our perspective is that the truncation in this prior is useful from a dimension reduction perspective because it avoids the number of groups increasing with sample size (Murugiah & Sweeting, 2012). Indeed, Casella et al. (2014) justified their use of a strong shrinkage prior by stating that, even when the true number of cluster is large, cluster analysis “will only result in useful inference when the answer contains a relatively small number of clusters.” For the same reason, we advocate for modelers interested in dimension reduction to carefully think about the maximum number of groups that is still manageable/interpretable when defining where to truncate the stick-breaking prior, this way limiting the complexity of the solution that is found by the algorithm.

The truncated stick-breaking prior for $\boldsymbol{\theta}$ is constructed indirectly by first defining

$$V_k \sim \text{Beta}(1, \gamma)$$

for $k = 1, \dots, K - 1$ and V_K is set to 1. The parameters V_1, \dots, V_K are then used to calculate θ_k , employing the following expressions:

$$\theta_1 = V_1$$

$$\theta_k = V_k \prod_{p=1}^{k-1} (1 - V_p) \text{ for } k > 1. \quad (1)$$

We use the following shorthand to denote this prior:

$$\boldsymbol{\theta} \sim \text{TSB}(\boldsymbol{\gamma}).$$

Notice that, according to this prior, the expected proportion of units assigned to cluster k is given by

$$E[\theta_k] = E[V_k] \prod_{p=1}^{k-1} (1 - E[V_p]) = \frac{1}{1 + \gamma} \left(1 - \frac{1}{1 + \gamma}\right)^{k-1}$$

$$= \frac{\gamma^{k-1}}{(1 + \gamma)^k} \text{ for } k < K; \text{ and}$$

$$E[\theta_k] = \left(1 - \frac{1}{1 + \gamma}\right)^{k-1} \text{ for } k = K.$$

The depiction of this equation for $0 < \gamma < 1$ reveals an approximately exponential decay of $E[\theta_k]$ with increasing k and that smaller γ corresponds to faster decay and therefore sparser results (i.e., fewer clusters).

To illustrate how this prior works, say we have a maximum of six groups ($K = 6$) and $\mathbf{V} = [V_1, \dots, V_6]$ is equal to $[0.19, 0.33, 0.27, 0.95, 0.47, 1.00]$. Recall that, by definition, V_6 is set to 1. As illustrated in Table 1, these values for \mathbf{V} imply that $\boldsymbol{\theta} = [\theta_1, \dots, \theta_6]$ is equal to $[0.19, 0.27, 0.15, 0.38, 0.01, 0.01]$. Note that θ_5 and θ_6 are very small compared to $\theta_1, \dots, \theta_4$ and that the four first groups account for 99% of all observations. These values suggest the presence of four main groups, despite having allowed for up to six groups. These results arise because the TSB prior shrinks θ_k to 0 for large values of k . Similar to how the components that only explain a small portion of the variation are typically ignored when conducting a Principal Component Analysis (PCA), the remaining groups when using the TSB prior (i.e., groups 5 and 6) are also typically ignored.

An intuitive way of interpreting the expressions for θ_k in Table 1 is to think about a sequential process in which a sampling unit is eventually assigned to cluster k after failing to be assigned to clusters $1, 2, \dots, k - 1$. For example, the expression for θ_3 can be interpreted as the probability that a sampling unit is not assigned to group 1 (equal to $1.00 - 0.19$) times the probability that it is not assigned to group 2 (equal to $1.00 - 0.33$) times the probability that it is assigned to group 3 (equal to 0.27). The

TABLE 1 Example of the calculations involved in the truncated stick-breaking prior assuming a maximum number of six cluster

Cluster	V_k	θ_k
1	0.19	0.19
2	0.33	$0.33 (1 - 0.19) = 0.27$
3	0.27	$0.27 (1 - 0.33) (1 - 0.19) = 0.15$
4	0.95	$0.95 (1 - 0.27) (1 - 0.33) (1 - 0.19) = 0.38$
5	0.47	$0.47 (1 - 0.95) (1 - 0.27) (1 - 0.33) (1 - 0.19) = 0.01$
6	1 (by definition)	$1 (1 - 0.47) (1 - 0.95) (1 - 0.27) (1 - 0.33) (1 - 0.19) = 0.01$

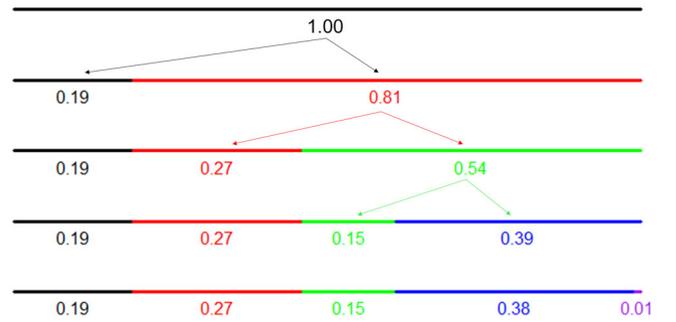


FIGURE 1 Visual representation of the stick-breaking metaphor. From top to bottom, one starts with a stick of length 1, breaking it into two sticks of length 0.19 and 0.81 (black and red). This latter piece (red) is then broken again into two sticks of length 0.27 and 0.54 (red and green). This latter piece (green) is then broken into two sticks of length 0.15 and 0.39 (green and blue). This process is reiterated multiple times until the maximum number of groups is reached

name “stick-breaking” originates from the metaphor of sequentially breaking a stick of length 1 into smaller and smaller pieces, as illustrated in Figure 1.

Another benefit of using the TSB prior is that, by weakly identifying the labels of each cluster, it can help to reduce the amount of label switching, a common problem for mixture models, which refers to the fact the group labels are unidentified parameters in these models. This problem often leads to poor mixing of MCMC algorithms and generates potentially nonsensical results if posterior distributions of parameters are summarized by their averages (Stephens, 2000).

Clustering models

To illustrate the wide applicability of the TSB prior, we describe three probabilistic partition clustering methods that greatly benefit from this prior. All of these clustering

models have an observational model in which the response variable y_i , conditioned on the latent cluster membership variable z_i , comes from a distribution that has some parameters indexed by z_i . More explicitly, we assume that

$$y_i|z_i = k \sim f(\beta_k, \phi)$$

where β_k is the set of cluster-specific parameters and ϕ is a vector containing the remaining parameters that are not cluster specific. We specify $f()$ and the priors for β_k and ϕ in greater detail when describing the individual models used to illustrate the TSB prior. In all models, we assume that the latent cluster membership variable z_i is given by

$$z_i \sim \text{Cat}(\theta)$$

and that

$$\theta \sim \text{TSB}(\gamma).$$

A commonly used prior for γ is a Gamma distribution (Dunson & Xing, 2009; Manrique-Vallier, 2016; Si & Reiter, 2013). However, we decided to adopt a discrete uniform prior for γ , where this parameter can take any of the following values 0.1, 0.15, 0.2, ..., 0.95, and 1.00 with equal probability. This prior was chosen because it ensures $\gamma \leq 1$, it is straightforward to implement, conforms to our prior belief of equal probability for all possible values of γ , and resulted in good mixing of our MCMC algorithms. Because of the truncation in the stick-breaking prior, $\gamma \leq 1$ ensures that the last group will be smaller than all the other groups (i.e., $E[\theta_k] > E[\theta_K]$ for $k = 1, \dots, K - 1$). All models were fit using Gibbs samplers and detailed information regarding the full conditional distributions (FCDs) used by these algorithms is given in Appendix S1.

Extensive simulations are used to show how the TSB prior can be used within these models to successfully estimate the true number of groups without requiring the fitting of multiple models with different numbers of groups. For all simulated data sets, we vary the true number of groups K and set the parameters within the vector θ to $1/K$, resulting in clusters of approximately equal size. We estimate the true number of groups by calculating the minimum number of groups that together represent more than 99% of all observations. More specifically, we assumed that the estimated number of groups \hat{k} is given by $\min_k \left(\sum_{j=1}^k \hat{\theta}_j > 0.99 \right)$, where $\hat{\theta}_j$ is the posterior mean for group j . Finally, because of the large number of simulations and the large number of parameters within any given model, we assessed convergence by examining

trace plots of the log-likelihood instead of trace plots of individual parameters.

Mixture model applied to movement ecology

Model description

Hidden Markov models (HMMs) have been extensively used to identify latent behavioral states (e.g., encamped, area restricted search, and transit) based on metrics derived from GPS location data, such as step lengths and turning angles (Morales et al., 2004). The estimation of latent states is valuable to the understanding of animal movement patterns since these states can be used to characterize the function of movements across a landscape when organisms are not directly observable (McClintock et al., 2020; Patterson et al., 2017; Wittemyer et al., 2019). By evaluating behavior-specific movements in relation to environmental covariates, mechanistic drivers of movement and measures of habitat suitability can be discerned from a variety of models, such as resource (Manly et al., 2002) or step-selection functions (Abrahms et al., 2016; Fortin et al., 2005; Wilson et al., 2012; Wittemyer et al., 2019). These latent states can also be used to infer activity budgets, providing a link to an animal's relative energy expenditure (Attias et al., 2018; Christiansen et al., 2013; McClintock et al., 2013; Wilmers et al., 2017; Wilson et al., 2020).

Similar to HMMs, our model also identifies these latent behavioral states, but it does not rely on a Markovian assumption or an underlying mechanistic movement process (e.g., correlated random walk). As a result, our model is better described as a mixture model instead of an HMM. Furthermore, instead of using the probability density functions typically adopted to model step lengths (e.g., gamma and Weibull) and turning angles (e.g., von Mises and wrapped Cauchy), we discretize these data and use a conditional categorical distribution as the likelihood. While discretizing the data arguably results in the loss of some information content, this approach has the benefit of being able to represent standard and non-standard distributions. This is important because parametric models can be prone to model misspecification (Diana et al., 2020) and it has been shown that relatively minor discrepancies between the data and the standard distributions often adopted within HMMs can lead to the identification of additional but superfluous latent states (Pohle et al., 2017). We believe that the flexibility in representing the distributions of step lengths and turning angles outweighs the relatively minor loss of information, particularly in the context of the large number of observations that arise from these GPS sensors.

Let $y_i^{(1)}$ and $y_i^{(2)}$ denote the step length and turning angle bins, respectively, that observation i falls into. We assume that

$$y_i^{(1)} | z_i = k \sim \text{Cat}(\Phi_{k1})$$

$$y_i^{(2)} | z_i = k \sim \text{Cat}(\Phi_{k2})$$

where $z_i = k$ is the latent cluster memberships of observation i for data type 1 and 2, respectively. The vectors Φ_{k1} and Φ_{k2} contain the probability that step lengths and turning angles, respectively, fall in each bin given that these observations were assigned to cluster k . Finally, our priors are

$$\Phi_{k1} \sim \text{Dirichlet}(a)$$

$$\Phi_{k2} \sim \text{Dirichlet}(a).$$

We assume a relatively sparse prior Dirichlet distribution for Φ_{k1} and Φ_{k2} by setting a to 0.1.

Simulated movement data

We systematically varied the number of clusters K from 2 to 10 and simulated 10 data sets for each setting. We assumed that both step lengths and turning angles were discretized into 15 bins. Each simulated data set contained 15,000 observations closely following the generative model described under ‘‘Model Description’’. To ensure that each cluster was sufficiently distinct from the other clusters, we relied on a discretized normal distribution for Φ_{k1} and Φ_{k2} . We assumed that the means were evenly distributed across the 15 bins and that the standard deviation was one-fourth of the distance between means. For example, for three clusters, this discretized normal distribution peaked at the 1st, 8th, and 15th bins, respectively, and the standard deviation was equal to $(8 - 1)/4 = 1.75$. Finally, we set the maximum number of groups to 15 and ran the Gibbs samplers for 10,000 iterations for each simulated data set.

Empirical movement data

We rely on GPS telemetry data from 20 individuals of the southern three-banded armadillo (*Tolypeutes matacus*), a species classified as Near Threatened (A2cd) by the IUCN Red List of Threatened Species and highly prioritized for conservation in Brazil (ICMBio, 2014). These data were

collected from two sites in the Pantanal wetlands of Brazil using a GPS tracking device with approximately 5-minute interval fixes. For each captured individual, age, sex, reproductive status, and body mass were measured. Additional information regarding this system and data can be found in Attias et al. (2020).

Location errors and missing location fixes are widely acknowledged problems with GPS location data (Bjorneraas et al., 2010; Ranacher et al., 2016). To properly analyze these data, we used a number of filtering steps. First, we excluded the data that were collected while armadillos were in their burrows, usually during the daytime, since no movements occurred during this time. Second, we only retained measurements at 5 ± 1 minute intervals to ensure that the derived speed and turning angles were comparable. Speed was calculated as step length divided by the time interval (i.e., the amount of time between successive GPS fixes) and turning angle was calculated as the change in direction between successive steps. Finally, we removed observations for which speed was greater than the 99.9% percentile (equal to 0.71 m/s) to remove biologically implausible movements. After all of these filtering steps, our final data set contained 13,671 observations from 20 individuals. Speed was discretized into bins of equal widths (0.1 m/s) up to 0.6 m/s with the final bin containing all observations >0.6 m/s, resulting in 7 bins. Turning angle was discretized into 10 evenly spaced bins between $-\pi$ and π .

We set the maximum number of groups to 15 and ran our Gibbs sampler for 20,000 iterations, discarding the first one-half of the iterations as burn-in. Besides identifying and characterizing each behavioral state, the goal of this analysis was also to gain insights regarding the basic ecology of this poorly known species. To this end, we explore how different factors influence the probability of each behavioral state using a post-hoc generalized linear mixed model (GLMM) with random effects for each individual using the R package *lme4* (Bates et al., 2015). In addition to the individual level information from the armadillos, we include time of day, ambient temperature, and precipitation as additional predictor variables. Temperature and precipitation are based on daily averages obtained from automatic stations of the Brazilian National Institute of Meteorology (INMET), located in the municipality of each study site. Differently from the clustering process, in which a single model was fit to data from both sexes, we fitted separate GLMM models for females and males. In these models, random effects were included for each individual. It is important to note that uncertainty from the mixture model is not appropriately propagated to the GLMM parameter estimates. However,

we believe that this model can still be useful in helping to interpret the results from the mixture model.

Mixture model applied to species occurrence data (i.e., biogeographic region model)

Model description

In this section, we focus on the clustering of locations with similar species composition. These locations are often spatially clustered, resulting in areas that have been variously called biogeographical regions (BR), bioregions, regions of common profile, forest types, or bird conservation regions in the literature. The delineation of these areas is a common task in ecology because it has important implications for both basic and applied scientific questions, such as those in historical biogeography, conservation, and natural resources management (Hill et al., 2017; Kreft & Jetz, 2010; Vilhena & Antonelli, 2015). A review of methods to delineate these areas is provided in Hill et al. (2020).

Let y_{is} denote the number of times that species s ($s = 1, \dots, S$) was seen in location i ($i = 1, \dots, n$). We assume that y_{is} arises from a Binomial distribution given by

$$y_{is} | z_i = k \sim \text{Binomial}(n_i, \phi_{ks})$$

where z_i is the latent group membership and n_i is the number of observation opportunities in location i . Notice that z_i influences this Binomial distribution by determining the subscript of the parameter ϕ_{ks} , where $k = 1, \dots, K$. The parameter ϕ_{ks} represents the presence probability of species s if location i belongs to cluster k . Therefore, the vector $[\phi_{k1}, \dots, \phi_{kS}]$ characterizes cluster k in relation to its species composition. Finally, we adopt the following priors:

$$\phi_{ks} \sim \text{Beta}(a, b).$$

We assume that $a = b = 1$, resulting in a uniform prior for ϕ_{ks} .

Simulated biogeographic data

The true number of groups K was set to 2, 4, 8, 16, and 32 for this model. Ten data sets were generated for each setting and all simulated data sets had 2679 locations and 443 species, similar to the bird data set that was used

for one of our case studies. We generated the simulated data closely following the generative model described in the “Model Description” section. To retrieve the true number of groups, we set the maximum number of groups to 50 and ran the Gibbs samplers for 1000–5000 iterations for each simulated data set.

Empirical biogeographic data

The Alberta Biodiversity Monitoring Institute (ABMI) monitors large-scale responses of biodiversity to environmental change in Alberta, Canada. The program reports on the status and trends of species by establishing species–habitat relationships, determining species’ response to various land-use changes, and producing predictive maps. The information on the trend and status of biodiversity, derived from these species-specific results, is then used to support natural resource and land-use decision making in Alberta. While species-specific models are typically created, results are often summarized across species depending on their shared response to natural or human disturbance (e.g., forestry, agriculture) to highlight major results that can be of particular interest in a given region.

The goal of this analysis is to identify the major plant communities in the forested and prairie regions of Alberta, enabling the characterization of biodiversity across large spatial scales. These results are useful in summarizing the response patterns to disturbances of a large number of species, helping to convey the results (display, interpret, and explain) to land-use managers. We used presence/absence data on vascular plant species in Alberta collected by the ABMI. Sites surveyed by ABMI in terrestrial habitat were spaced throughout Alberta using the 20-km National Forest Inventory grid. At each site, a 100×100 m survey area was established and each survey area was further divided into four 50×50 m square plots. Because our model lumps these four square plots together, the number of observation opportunities in survey area i (i.e., n_i) is equal to 4 and the number of times species s was seen in this survey area (i.e., y_{is}) is an integer between 0 and 4. All vascular plant species in these plots were identified and their presence/absence in each of these plots was recorded. We focused on data from 2007 to 2018 because of the consistent data collection protocol from this period of time. We also eliminated data from very rare species, defined as species that were present in less than 1% of the sites, resulting in a final data set with a total of 1082 sites and 351 species. Details about data collection can be found in ABMI (2014).

The maximum number of groups was set to 50 and the Gibbs sampler was run for 10,000 iterations, discarding the first one-half of the iterations as burn-in. To enable the visualization of the spatial distribution of the identified clusters, we fit post-hoc Bayesian logistic regressions to the results from the BR model and then use these regression models to create spatial predictions. Predictor variables for these logistic regressions included two climate variables (i.e., mean annual temperature and precipitation) and percentage of land area covered by nine habitat types (i.e., deciduous forest, pine forest, white spruce forest, mixed wood forest, black spruce forest, fens with trees, swamps with trees, open wetland [fen/marsh], and grass/shrub), and five types of anthropogenic landscapes (i.e., harvested forest stands, vegetated strips along linear features [e.g., trails, roads, and railways], crops/pastures, urban industrial/mines, and paved and gravel roads). We considered these variables because they are biologically meaningful and are available throughout the entire study area at the spatial scale of 1 km². Similarly to our analysis of the mixture model results applied to the movement data, it is important to note that uncertainty from the BR model is not appropriately propagated to the logistic regression parameter estimates. However, we believe that the derived maps based on this logistic regression can still be useful in helping to interpret the results from this mixture model.

Species archetype models

Model description

Species archetype (SA) models were originally developed by Dunstan et al. (2011) to cluster species that responded similarly to environmental gradients (i.e., species that had similar regression parameters). While the original model followed a relatively standard mixture of regression models approach (Grun & Leisch, 2008), this model was subsequently improved by allowing each species to have a separate intercept (Dunstan et al., 2013), enabling species-specific differences in overall prevalence.

Species archetype models have been put forward as a potentially effective strategy to group species, resulting in species archetypes (i.e., groups of species that respond in a similar fashion to the environment; Dunstan et al., 2011; 2013; Hui et al., 2013). Furthermore, SA model results can also simplify conservation management decision by enabling managers to focus on a small set of species archetypes, instead of having to evaluate a multitude of species, each with their own idiosyncratic response to the environment (Dunstan et al., 2011; 2013; Hui et al., 2013).

Let y_{is} denote the presence (1) or absence (0) of species s ($s = 1, \dots, S$) in location i ($i = 1, \dots, n$). Because this is a binary variable, we assume the following Bernoulli distribution:

$$y_{is} | z_s = k \sim \text{Bernoulli}(\Phi(\alpha_s + \mathbf{x}_i^T \boldsymbol{\beta}_k))$$

where z_s is the latent cluster membership of species s , α_s is a species-specific intercept, \mathbf{x}_i^T is a vector of location-specific covariates, $\Phi()$ is the standard normal cumulative distribution function, and $\boldsymbol{\beta}_k$ is a vector containing the regression slopes for cluster k , where $k = 1, \dots, K$. Notice that the latent variable z_s influences this Bernoulli distribution by determining the subscript of the vector $\boldsymbol{\beta}_k$. In other words, species that belong to the same cluster k have the same slope parameters $\boldsymbol{\beta}_k$, essentially having identical responses to covariates. We adopt a probit link (instead of the more common logit link) because it enables the straightforward fitting of the model using the data augmentation scheme described in Albert and Chib (1993). More specifically, we assume the existence of another set of latent variables ω_{is} such that

$$y_{is} = 1 \quad \text{if } \omega_{is} > 0$$

$$y_{is} = 0 \quad \text{otherwise}$$

where

$$\omega_{is} \sim N(\alpha_s + \mathbf{x}_i^T \boldsymbol{\beta}_k, 1).$$

For the remaining parameters, we adopt the following priors, given by

$$\alpha_s \sim N(0, 10)$$

$$\boldsymbol{\beta}_k \sim N(\mathbf{0}, \mathbf{I})$$

where \mathbf{I} is the identity matrix.

Simulated data

Similar to the BR model, the true number of groups K was set to 2, 4, 8, 16, and 32 for this model. Ten data sets were generated for each setting and, similarly to the empirical data, all simulated data sets had 2679 locations and 443 species. We generated the simulated data closely following the generative model described in the ‘‘Model description’’ section. Furthermore, we simulated the

slope parameters β_k from standard normal distributions. However, to simulate the species-specific intercepts, we assumed that $\alpha_s \sim N(0, 0.4^2)$. The standard deviation for α_s was set to 0.4 to avoid creating data in which certain species are almost always present or almost always absent. This is important because it would be difficult for our models to assign these species to their correct groups given that this assignment depends on the accurate estimation of the slope parameters β_k . We also assumed that six uncorrelated covariates were available, which were generated from standard normal distributions. The maximum number of groups was set to 50 and the Gibbs samplers were run for 1000–5000 iterations for each simulated data set.

Empirical data

The Breeding Bird Survey (BBS) is a long-term program that monitors the status and trend of bird populations in North America. In brief, data are collected annually in June by trained participants along randomly established roadside routes approximately 39 km long with stops 0.8 km apart. At each stop, a 3-minute point count is conducted (Pardieck et al., 2017).

The BBS actually records count data (rather than presence/absence) per stop in each route. However, these counts may include the same individual observed multiple times and bird detection may vary by species and environmental conditions (e.g., weather or traffic noise). To avoid some of the issues with the count data and to be able to illustrate the use of the SA model described in the “Model description” section, we convert these count data into presence/absence of each species in each route. Furthermore, we subset the BBS data for the year of 2015 and eliminate data from very rare species, defined here as species that were present in less than 10 routes. In total, the final data set used for analysis contained information on 443 species and 2679 routes, spread throughout Canada and the United States.

To understand how bird species are affected by climatic variables, we gathered average temperature and precipitation for North America from 1970 to 2000 for the month of June from WorldClim, with a spatial resolution of 5 arc-minutes (10 km grid; www.worldclim.org/version2). Because each species archetype can potentially have non-linear associations with precipitation and temperature, we relied on B-splines to capture the association between these environmental variables and species presence. More specifically, B-spline basis functions were included in the model for temperature and

precipitation, where knots were a priori set to 10%, 20%, ..., 90% percentiles of the corresponding environmental variables. Additional information regarding different types of splines and basis functions can be found in Wood (2017) and similar functional clustering ideas can be found in Dunson (2010). By identifying the niche breadth in relation to temperature and precipitation of the different species groups, this analysis is able to identify which of these groups are more likely to be impacted by changes in precipitation, changes in temperature, or changes in both variables. We set the maximum number of groups to 50 and ran our Gibbs sampler for 10,000 iterations, discarding the first one-half of the iterations as burn-in.

Software

To enable readers to reproduce the results described in this article and to use the different models highlighted here for their own data, we have created an R package called EcoCluster that enables straightforward fitting of the BR model and the SA model, both with the TSB prior. We have also created an R package called bayesmove (Cullen et al., 2021) that enables the straightforward fitting of the mixture model with the TSB prior used for the movement data. These packages are *available online* (<https://doi.org/10.5281/zenodo.5683639>; <https://CRAN.R-project.org/package=bayesmove>). The vignettes accompanying these R packages illustrate how to fit these models and interpret their results.

RESULTS

Simulated data results

We find that the proposed models with the TSB prior are able to successfully recover the true number of groups for all models, with a slight decrease in performance for the BR model when the true number of groups is equal to 32 (top panels in Figure 2). Importantly, we find that the data contain substantial information on γ (the parameter that governs the TSB prior), with posterior means for γ that are relatively small for sparse settings (i.e., when only few groups exist) vs. closer to 1 when many groups exist (bottom panels in Figure 2). We also find that all of the proposed algorithms were able to accurately retrieve the parameter values used to simulate the data (i.e., Φ_{k1} and Φ_{k2} for the mixture model applied to the movement data, ϕ_{ks} for the BR model, and α_s , β_k for the SA model; data not shown).

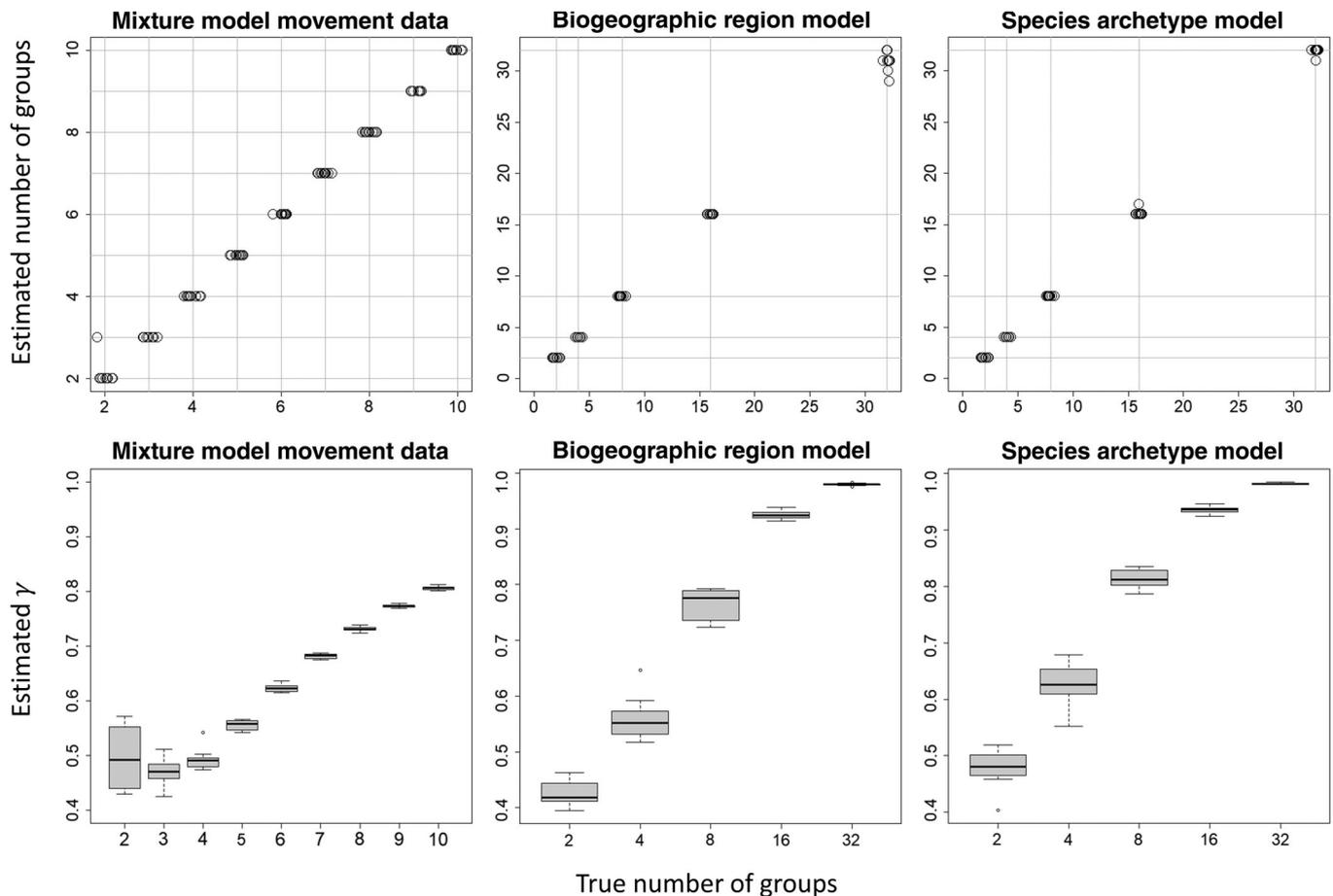


FIGURE 2 The use of the truncated stick-breaking (TSB) prior in the different model enables the successful uncovering of the true number of groups (top panels) and these simulated data contain considerable information regarding the hyper-parameter of the TSB prior γ (bottom panels). Left to right panels show the estimated number of groups (top panels) and the estimated γ (bottom panels) for the mixture model applied to the movement data, the biogeographical regions (BR) model and species archetype (SA) model, respectively, based on 10 simulated data sets for each value of the true number of groups. We assumed a maximum of 15 groups for the mixture model applied to the movement data, and a maximum of 50 groups for the BR and SA models. Notice that the x-coordinate of each point was shifted slightly (i.e., jittered) on the top panels to enable the visualization of overlapping circles

The standard approach of fitting models with different number of clusters and then selecting the optimal number of clusters is much more computationally expensive. For example, using the real data sets, we found that the time required to fit the mixture model with the TSB prior applied to movement data and a maximum of 15 groups was equal to 17% (25 minutes vs. 149 minutes) of the time needed to fit multiple mixture models, one for each number of clusters (2–15). Similarly, fitting the BR model once with the TSB prior and a maximum of 50 groups corresponds to approximately 6% (10 minutes vs. 189 minutes) of the total time required to vary the number of clusters from 2 to 50 and fit individual BR models for each setting. Finally, fitting the SA model once with the TSB prior and a maximum of 50 groups took 4% (40 minutes vs. 990 minutes) of the time required to run multiple SA models, one for each prespecified number of clusters (2–50).

Empirical results for the mixture model applied to movement data

Our model identified two behavioral states (out of a maximum of 15 possible states) that together comprise 99% of all observations. The first state is comprised mostly of slower and more tortuous movements (hereafter “foraging” state, Figure 3a,b) while the second state includes faster and more directed movements (hereafter “transit” state, Figure 3c,d). When exploring these results, we find that, while the daily number of observations assigned to the foraging state is very similar between males and females (Figure 3e), males tend to have a higher number of observations assigned to the transit state (Figure 3f). To determine how covariates influence these behavioral states, we fit a post-hoc GLMM, where the binary response variable was equal to 1 for the transit state and

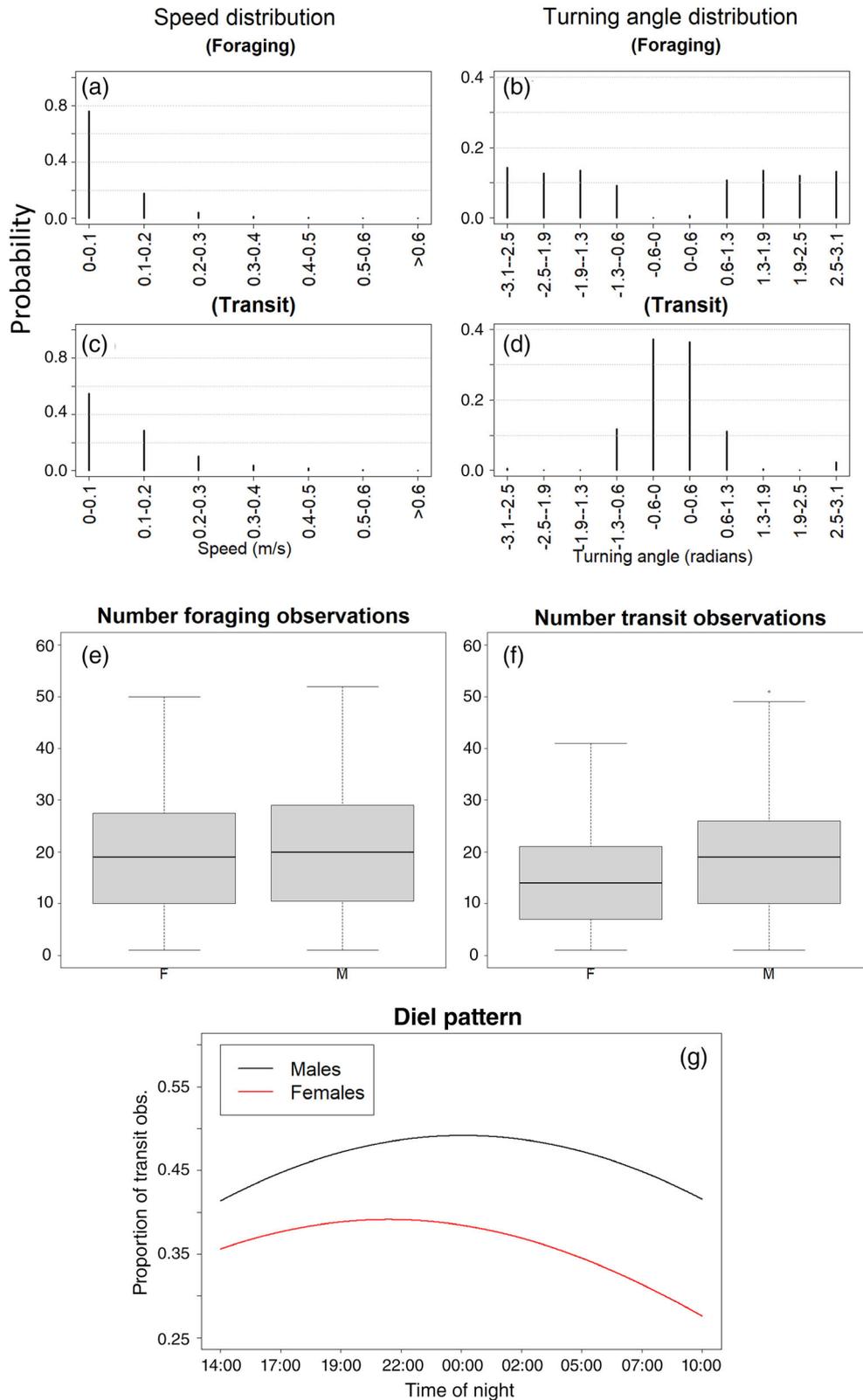


FIGURE 3 Results for the mixture model applied to movement data. Panels a–d depict the estimated distributions for speed and turning angle for the two behavioral states identified by the mixture model. The first state, henceforth “foraging,” is characterized by slower and more tortuous movements (panels a and b) while the second state, henceforth “transit,” is characterized by faster and more directed movements (panels c and d). Comparisons are made between females (F) and males (M) regarding the daily number of observations assigned to the foraging state (panel e), and the daily number of observations assigned to the transit state (panel f), and the estimated proportion of transit observations as a function of time of night (panel g)

0 otherwise. The larger proportion of the transit state for males in comparison to females is evident by the much larger intercept for males when compared to females (Table 2). Furthermore, we find a quadratic relationship between the probability of exhibiting the transit state with time of night (Figure 3g). Finally, we do not find a strong influence of precipitation, temperature, or region on the proportion of the transit state (Table 2). These results suggest that armadillos from both regions behave similarly and that precipitation/temperature have no measurable effect on the proportion of the transit state despite the fact that decreased daily temperatures have been associated with an overall lower duration of activity period (Attias et al., 2018).

Empirical results for the BR model applied to the vascular plant data from Alberta

The BR model identified seven (out of 50) major groups, representing 99.5% of all locations. This analysis resulted in substantial dimension reduction given that, instead of having to separately examine the results for 351 species, the BR model enables us to focus just on the results from these seven groups. To simplify the interpretation and enable the spatial visualization of the patterns identified by the BR model, we fitted a post-hoc logistic regression to the results from this model. Predictions from these regression models reveal striking spatial patterns (Figure 4). For example, group three had a strong association with temperature and precipitation, with most species in this group being relatively rare species that are mainly restricted to the colder Rocky Mountains, Upper Foothills, and Canadian Shield natural regions (e.g., Engelmann spruce *Picea engelmannii* and Rocky Mountain alpine fir *Abies bifolia*). On the other hand, group 2 had a positive association with most of the other remaining upland forest types (i.e., deciduous, white spruce, mixed wood, and harvested stands). Groups 4 and 5 were mostly restricted to lowland forest types (black spruce and fens with trees). Interestingly, group 1 was strongly associated with the proportion of cultivated land (e.g., crop and pasture), agreeing with the fact that many of the species that dominate this group are either introduced or cultivated species (e.g., canola *Brassica napus* and barley *Hordeum vulgare*). Group 7, on the other hand, was strongly associated with highly anthropogenic landscapes, with substantially increased presence probabilities in regions with higher urban/industrial/mines areas and associated vegetated strips along railways, roads and trails (soft-linear). The characteristic species in this group include white sweet clover *Melilotus albus*, yellow sweet clover *M. officinalis*, and scentless chamomile *Tripleurospermum inodorum*.

Empirical results for the SA model applied to the breeding bird survey data

All of the 50 species groups in the SA model had species in them but 95% of all the species were contained in the first 40 of these groups. As expected, several groups were strongly associated with temperature and/or precipitation, typically exhibiting unimodal relationships between average prevalence and these environmental variables. An example of the results for four species groups are shown in Figure 5. The results for all the other species groups are available in Appendix S2.

The line graphs in Figure 5 illustrate how all the species within a species archetype respond in a similar fashion to the environment. The heat maps of the predicted average prevalence for different combinations of temperature and precipitation provide a depiction of the environmental space occupied by these species groups (i.e., the realized niche, Figure 5). These figures illustrate that some species archetypes are relatively insensitive to precipitation but very sensitive to temperature (e.g., species archetype 31), some are relatively insensitive to temperature but very sensitive to precipitation (e.g., species archetype 5), while some groups are sensitive to both temperature and precipitation (e.g., species archetype 21). These results can potentially be useful to highlight which sets of species are more likely to be impacted by different facets of climate change (Tingley et al., 2012), enabling the prioritization of these species for conservation purposes.

DISCUSSION

Determining the number of clusters is a long-standing challenge for a range of clustering algorithms. The standard approach to deal with this problem for model-based clustering consists of fitting models with different number of groups and selecting the optimal number of groups using indices such as AIC or BIC, an approach that can be very computationally intensive and that has been reported to often overestimate the true number of groups. Here we show how Bayesian clustering models, when used in conjunction with sparsity inducing priors such as the TSB prior described here, can determine the number of clusters without requiring the fitting of multiple models.

To illustrate how a wide range of Bayesian clustering models can benefit from sparsity-inducing priors, we show with simulated data how the truncated-stick breaking (TSB) prior can successfully estimate the true number of groups for three types of clustering models (i.e., two mixture models, one applied to movement data and the other applied to species occurrence data, and an SA

TABLE 2 Generalized linear mixed model (GLMM) regression coefficients

Parameters	Female		Male	
	Estimate	Pr(> z) ^a	Estimate	Pr(> z) ^a
Intercept	-0.47	0.000	-0.03	0.803
Time	-0.23	0.083	0.00	0.969
Time ²	-0.48	0.019	-0.49	0.030
Temperature	0.04	0.246	0.01	0.795
Precipitation	0.00	0.843	0.06	0.096
Region	0.25	0.063	0.03	0.872

Note: Statistically significant ($P < 0.05$) coefficients are highlighted in boldface type.

^aNote that P values should be interpreted with care because (a) the GLMM model assumes temporal independence within each individual, which is unlikely to be a valid assumption given that these data were collected every 5 minutes, and (b) uncertainty from the first-stage mixture model is not taken into account.

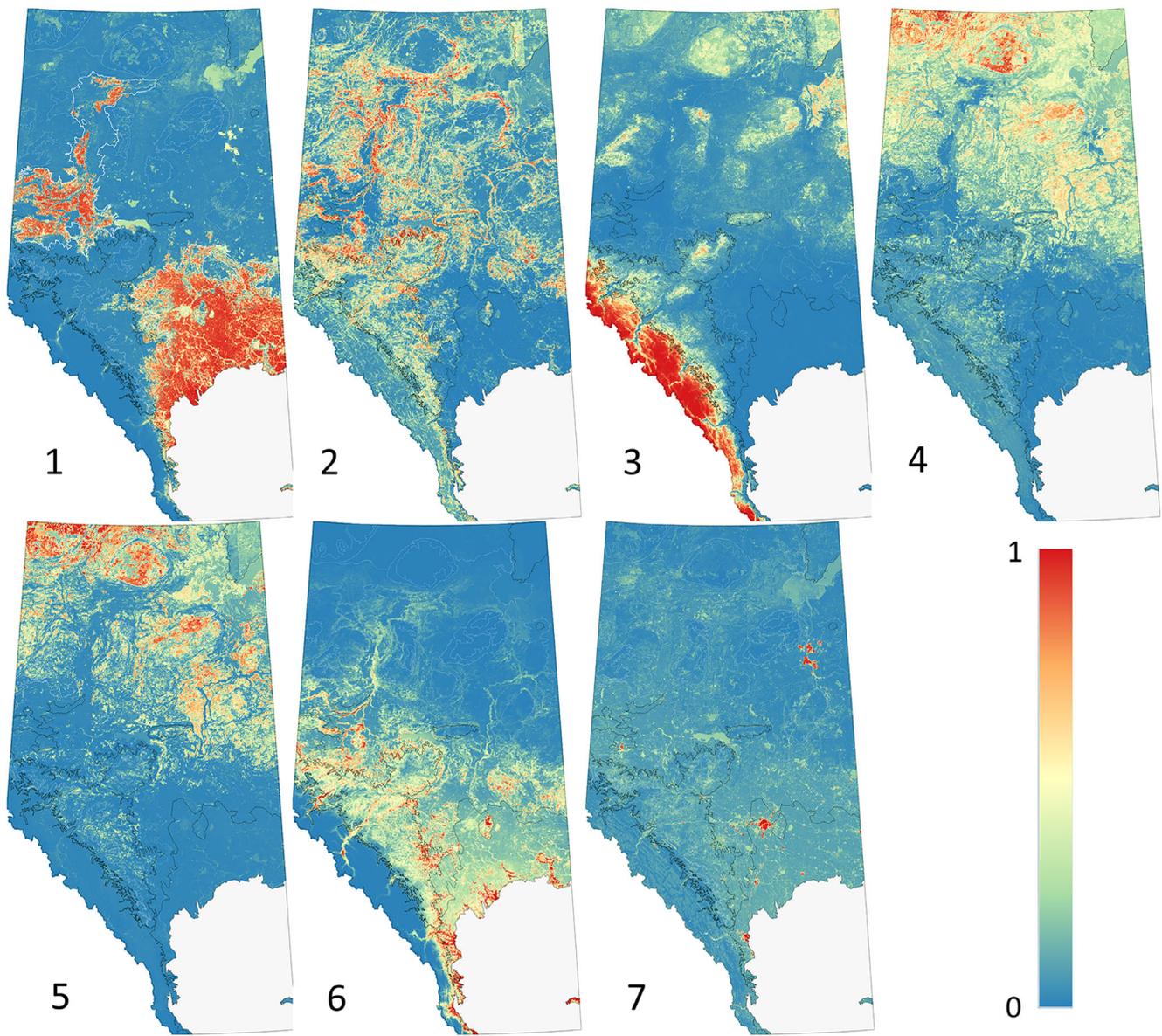


FIGURE 4 Spatial distribution of the groups identified by the biogeographic region model. Each panel depicts the predicted presence probability of each group, where cyan to purple indicate probabilities ranging from 0 to 1, respectively. Group numbers are given in the lower left corner of each map

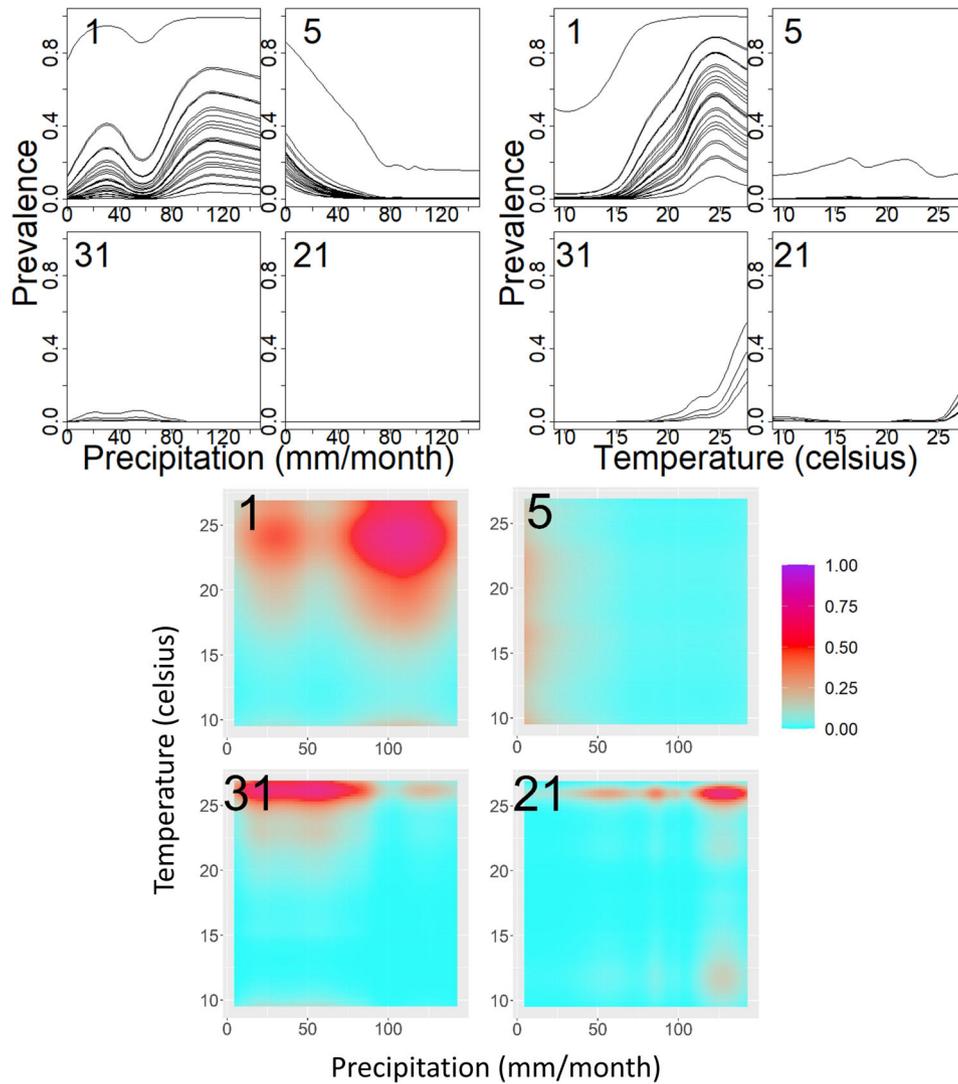


FIGURE 5 Association between occurrence probability (prevalence) and precipitation and temperature for a subset of the species archetypes identified by the SA model. Each panel displays the results for a particular species archetype (numbers in the top left corner correspond to the species archetype identifier). Individual lines in the line graphs depict the estimated associations for each species within that archetype. For the precipitation line graphs, temperature was set to its mean value. Similarly, for the temperature line graphs, precipitation was set to its mean value. Heat maps show the environmental space of each species archetype by displaying the average prevalence for each temperature and precipitation combination. In all panels, the ranges for precipitation and temperature were limited to the 2.5 and 97.5 percentiles from the original data. Cyan to purple indicate probabilities ranging from 0 to 1

model that clusters species according to how they respond to the environment). Nevertheless, we believe that the ability to identify the existing clusters is likely to depend on several factors, including the type of model, how distinctive the clusters are from one another, the size of each group, and the amount of available data. For example, additional simulations in which groups were allowed to vary in size revealed that the BR model did not perform as well as the other models in this setting (Appendix S3). A closer examination of the BR model results revealed that this model had a challenging time correctly assigning some of the plots to the rare groups (i.e., groups assigned to less than 10 plots) because these

groups were rare and therefore much harder to characterize. Additional research needs to be conducted to better characterize the circumstances in which the TSB prior is likely to work well and when it is likely to fail.

We also show that the standard approach of varying the number of groups and fitting multiple models is much more computationally expensive. Some might argue that using AIC or BIC based on fitting multiple models is only computationally problematic if the algorithms used to fit these models are slow (e.g., MCMC algorithms). Our experience has been that several of the alternative clustering models that rely on optimization (e.g., SAM and HMM in the *ecomix* and *momentuHMM* R

packages, respectively) instead of MCMC algorithms are also relatively slow because they often require multiple model fits for a given number of groups due to the multimodality of the likelihood surface. This is further exacerbated if different numbers of groups need to be tested and a bootstrapping approach is required to estimate parameter uncertainty (e.g., as in SAM within the *ecomix* package). As a result, despite the intuition that optimization algorithm will always be faster than MCMC algorithms, in practice this is not always true because of the multiple model fits that are required by these optimization-based methods.

We demonstrate how these models can unveil important environmental management and ecological insights. In the mixture model applied to the movement data from the three-banded armadillos, we identified two latent behavioral states, which were labeled foraging and transit. Additionally, we found that males tend to exhibit a greater proportion of time in the transit state than females and that the proportion of this state peaks mid-way through the night. These sexual differences regarding the transit state are likely related to the species' sociobiology, as the increased transit state of the promiscuous males should increase their chances of encountering receptive females. Indeed, males have been recently shown to have larger home ranges than females (Attias et al., 2020) and, according to our results, this difference is unlikely to be related to the acquisition of energetic resources by the larger males, as there were no noticeable differences in the amount of foraging state between sexes (Figure 3e).

The BR model enabled substantial dimension reduction by summarizing the results from 351 species into seven major groups. Similar to forest types and Bird Conservation regions, these results can be used for conservation and management purposes (https://data.fs.usda.gov/geodata/rastergateway/forest_type/; <https://nabci-us.org/resources/bird-conservation-regions/>). For example, our results have identified a plant community that is heavily influenced by anthropogenic disturbance. By mapping the spatial distribution of this group, our analysis can enable the spatial prioritization of restoration and invasive species elimination initiatives. Furthermore, the monitoring of this group is likely to be critical in identifying the main drivers of environmental change in the region and developing effective mitigation strategies.

In relation to the SA model applied to the 2015 survey data on North American breeding birds, we have identified species groups that respond similarly to temperature and precipitation. This enables the identification of sets of species that are likely to be more impacted by changes in precipitation, by changes in temperature, or by both.

Interestingly, differently from the other two applications, the SA model still identified the existence of 50 groups, which was the maximum number of groups allowed by our analysis. These results suggest that there are probably more groups than what we have allowed for in this analysis. We believe that this might be due to the flexibility of the environmental response curves and the relatively rigid structure of SA models, which require species to have the same set of slope parameters. As a result, relatively minor changes in how these species respond to their environment, particularly when there are a lot of observations for any given species, can foster the creation of many small groups instead of few large groups. Future research could devise a different formulation for the SA model so that species can be grouped together even if they differ slightly in how they respond to the environment. These results are also important to highlight that, despite the use of a sparsity-inducing prior, the model might still reveal that a sparse solution (i.e., a few clusters) is not supported by the data. In this situation, the modeler has to decide to either use the results as they are, because a larger number of groups would be unmanageable, or rerun the analysis with a larger number of groups.

An important limitation in our analysis of the armadillo movement data and the plant occurrence data from Alberta is that we relied on post-hoc regression models to better interpret our mixture model results. The problem with this two-stage approach is that it does not properly propagate the uncertainty associated with the mixture model results, potentially leading to over-confident inference and predictions. While this might not be too troublesome for exploratory studies like ours, this is an important problem for more confirmatory analyses. There are relatively few methods that have been developed that avoid these post-hoc analyses (see review in Hill et al., 2020). Nevertheless, the few existing single-stage methods require multiple models to be fit to determine both the optimal number of groups and the optimal set of covariates. Properly propagating the uncertainty associated with all these decisions is an area of active research even for these single-stage models.

It is important to note that, because our primary goal was to show the versatility of the TSB prior, we have not provided a more in-depth comparison of the three example models to other commonly used models. Such a model comparison could be useful future research. Furthermore, we have focused on ecological clustering applications, but the TSB prior is likely to be useful for a much broader range of applications (e.g., for use of the Dirichlet process for genetic clustering; see Huelsenbeck & Andolfatto, 2007). Also, we have focused on models where the primary interest is on the identified latent structure (i.e., the identified

clusters) because we believe that this is the type of dimension-reduction result that ecologists find more revealing and insightful. Indeed, many of the ecological applications involving the Dirichlet process and its extensions rely on the identified clusters to draw insights regarding, for example, animal movement and migration patterns (Diana et al., 2020; Valle et al., 2017), temporal dynamics of seal pup rookeries (Johnson et al., 2013), and spatial distribution of bird communities (Valle et al., 2018). However, we acknowledge that the Dirichlet process has been used for a much wider range of applications, some of which are not focused on identifying clusters. For example, in ecology, the Dirichlet process has been used for density estimation (Dorazio et al., 2008), to develop spatial models of the expected number of birds (Rodriguez & Dunson, 2011), and to generate a more parsimonious description of the covariance matrix between species in joint species distribution models (Taylor-Rodriguez et al., 2017).

It is important to note that our approach does not apply to all clustering methods. For instance, many clustering approaches are algorithmic and do not rely on an underlying statistical model, precluding the use of our approach. Even among clustering approaches based on statistical models, adopting a prior will only make sense for models fitted within a Bayesian framework. Finally, attempts to fit models with the TSB prior using packages such as JAGS (Plummer, 2003) and Stan (Stan Development Team, 2020) may result in label switching and convergence problems (Sollmann et al., 2020). The reason for this is that we have observed that a critical step for our customized MCMC algorithms to perform well is to order the identified clusters (from largest to smallest) during the burn-in phase. While this ordering does not change the likelihood (cluster labels are unidentified in standard mixture models), it does influence the TSB prior. Mixture models often have multimodal posteriors/likelihood functions (Scrucca et al., 2016; Stephens, 2000) and the ordering of clusters helps the model with the TSB prior find the highest peak, this way reducing label switching and convergence issues. Developing approaches for ordering clusters within packages, such as JAGS or Stan, is an important area for future research.

Despite the limitations described above, it is likely that clustering approaches will greatly benefit from sparsity-inducing approaches like the TSB prior in the same way that a wide range of regression models has benefitted from sparsity-inducing approaches (e.g., regularization penalties or strong priors) to improve predictions and identify the most important predictor variables (Hooten & Hobbs, 2015). Several extensions to this prior, already developed in Bayesian nonparametrics, may be profitably exploited in the future for clustering applications in ecology and environmental science. For example, the Pitman-Yor process (also

known as the two-parameter Poisson Dirichlet process; Pitman, 1995; Pitman & Yor, 1997) is a generalization of the Dirichlet Process that offers more flexible clustering rates and cluster size tail behaviors. Alternatively, a hierarchical Dirichlet process (Teh et al., 2006) could be used to capture nested clusters. Finally, a truncated stick-breaking prior together with a kernel based approach (Reich & Fuentes, 2007) could be used so that spatially proximate sites are more likely to cluster together, or a probit stick-breaking process (Rodriguez & Dunson, 2011) could be adopted to ensure that sites with similar environmental conditions and/or species with similar trait values are more likely to be clustered together.

Despite the fact that the stick-breaking prior has a relatively long history in statistics, relatively few ecological modelers have used this prior, probably due to the general lack of awareness among quantitative ecologists and environmental scientists regarding how this prior can help a wide range of applied clustering problems. This is particularly surprising given the prominent role of clustering methods in ecology and related disciplines (Legendre & Legendre, 2012). With this article, we hope to help remedy this situation by better characterizing the benefits of this approach while at the same time providing R packages that implement these methods, enabling the straightforward fitting of these models by quantitative scientists.

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CONFLICT OF INTEREST

The authors declare no conflict of interest.

AUTHOR CONTRIBUTIONS

Denis Valle conceived the ideas, designed the methodology, analyzed the data, and wrote the first draft of the article. Nina Attias provided the armadillo movement data. Nina Attias and Joshua Cullen helped to interpret the results from the mixture model applied to this movement data. Yusuf Jameel obtained the covariate data for

the SA model. Brenda Betancourt created the EcoCluster R package while Joshua Cullen created the bayesmove R package. Ermias T. Azeria provided the ABMI dataset and helped interpret the corresponding results. All authors contributed critically to the manuscript and gave final approval for publication.

DATA AVAILABILITY STATEMENT

Breeding Bird Survey data are based on the legacy format (Pardieck et al., 2017) available in the USGS ScienceBase-Catalog at: <https://doi.org/10.5066/P9YASED1>. Vascular plant data are available from the Alberta Biodiversity Monitoring Institute at <https://abmi.ca/home/data-analytics/da-top/da-product-overview/Species-Habitat-Data.html> by selecting “Vascular Plant” under “Species Variables” within “Terrestrial Variables.” Average temperature and precipitation data (Fick & Hijmans, 2017) are available from WorldClim at <https://www.worldclim.org/data/worldclim21.html> under “Historical climate data” and “5 minutes”. Armadillo movement data (Valle & Attias, 2021) are available on Figshare: <https://doi.org/10.6084/m9.figshare.17209175>.

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